

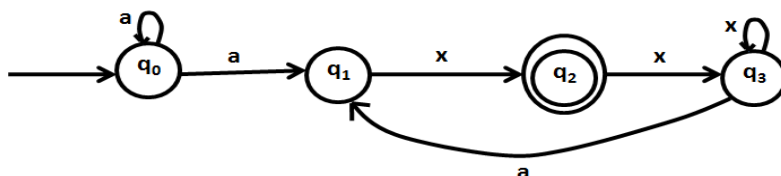
Note: All Questions from **PART-A** are to be answered at one place.

Answer any **FOUR** questions from **PART-B**. All Questions carry equal Marks.

PART-A

6 × 2 = 12M

1. Design a DFA to accept strings of a's and b's having even number of a's and b's.
2. For the NFA given below;
 - i. Check whether the string axxaxxa is accepted or not
 - ii. Give atleast two transition paths



3. Obtain a regular expression for $L = \{ VUV \mid U, V \in \{a,b\}^* \text{ and } |V| = 2 \}$.
4. Is the following grammar ambiguous?

$S \rightarrow AB \mid aaB$
 $A \rightarrow a \mid Aa$
 $B \rightarrow b$
5. Identify the nullable variables from the following CFG

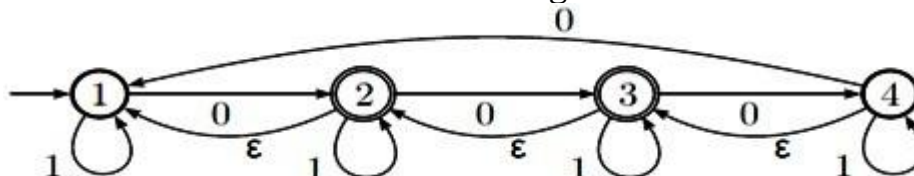
$S \rightarrow ABCa \mid bD, A \rightarrow BC \mid b, B \rightarrow b \mid \epsilon, C \rightarrow c \mid \epsilon, D \rightarrow d$
6. Explain individually classes P and NP.

PART-B

1. a) Construct a finite state automata that accepts those strings over $\{a,b\}$ that contains **aaa** as substring. (6M)
- b) Construct a DFA equivalent to $M = (\{q_0, q_1\}, \{a, b, c\}, \delta, q_0, \{q_1\})$ where δ is given in the following table. (6M)

δ	a	B	c
q_0	$\{q_0, q_1\}$	$\{q_1\}$	\emptyset
q_1	\emptyset	$\{q_0, q_1\}$	$\{q_1\}$

2. a) Construct a NFA without ϵ for the follwing NFA with ϵ . (6M)



- b) Construct a Mealy machine which is equivalent to the Moore machine given in table. (6M)

Present State	Next State		Output
	A=0	A=1	
→ q ₀	q ₃	q ₁	0
q ₁	q ₁	q ₂	1
q ₂	q ₂	q ₃	0
q ₃	q ₃	q ₀	0

3. a) Let G be the grammar. $S \rightarrow aS \mid aSbS \mid \epsilon$. Prove that $L(G) = \{x \mid \text{such that each prefix of } x \text{ has atleast as many a's as b's}\}$. (6M)
- b) Using pumping lemma show that the following sets are not regular:
- a) $\{a^n b^{2n} \mid n > 0\}$
- b) $\{a^n b^m \mid 0 < n < m\}$ (6M)
4. a) Eliminate epsilon productions from the grammar 'G' given as
- $A \rightarrow aBb \mid bBa$
- $B \rightarrow aB \mid bB \mid \epsilon$ (6M)
- b) Give CFG for generating odd palindromes over the string {a,b}. (6M)
5. a) Convert the following Grammar into CNF.
- $S \rightarrow AbcD \mid abc$
- $A \rightarrow aASB \mid d$
- $B \rightarrow b \mid cb$
- $D \rightarrow d$ (6M)
- b) Convert the following Context Free Grammar to Push Down Automata.
- $S \rightarrow aAA$
- $A \rightarrow aS \mid bS \mid a$ (6M)
6. a) Obtain a Turing machine to recognize $0^n 1^n 2^n$. Ex: 000111222..... (6M)
- b) Explain in detail about posts correspondence problem and 2-way infinite Turing machine. (6M)
